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# A hollow waveguide infrared thermometer for polymer temperature measurement during injection moulding

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### Abstract

We describe a novel on-line infrared method for remote sensing of the surface and the bulk temperatures of a polymer film during injection moulding. The method may also be applied to other polymer forming processes such as extrusion and blow moulding. The key feature of the new method is the use of a hollow waveguide that is incorporated into the injection mould to transmit the thermal radiation from the target to the sensor. The main characteristic of the hollow waveguide is that it exhibits low transmission loss of the thermal energy in the mid- and far-infrared, and no end reflection. This allows measurement of quite low temperatures, as low as near room temperature. Conventional optical fibre thermometers can neither measure such low temperature ranges nor measure the polymer surface temperature. In this paper, we present the first on-line results of critical tests of the new device. A Husky injection moulding press was used for the experiments. Good correlation was found between the radiometric results and those obtained with a thermal sensor inserted near the polymer mould interface, and with infrared imaging after the polymer part was ejected from the injection mould.

Keywords: Pyrometer, sensor, remote, optical, polymer, process

(Some figures in this article are in colour only in the electronic version)

# 1. Introduction

In polymer processes such as extrusion, injection moulding or blow moulding, the material undergoes a complex history in which it is melted, flows through complex geometries where viscous dissipation, shrinkage and warpage play a central role, is deformed to take the shape of the mould, and finally is cooled down and solidified into the final product. In all these processes, temperature distribution in the polymer is extremely complex and has a significant effect on the properties of the final part as well as the cycle time. Temperature is probably one of the most important parameters in polymer forming. However, its measurement is extremely difficult. One of the difficulties is the nature of the processes in which the material moves and solidifies to form the product so that invasive techniques such as thermocouple insertion are not

applicable. Another difficulty is the existence of non-uniform temperature throughout the melt thickness [1, 2]. Products that are moving or too fragile to touch are easily measured with non-contact techniques. Previous attempts to remotely measure the temperature include the use of fluorescence spectroscopy [3], ultrasonics [4], and infrared pyrometry [5]. In the fluorescence spectroscopy method, a temperaturesensitive dye is incorporated into the polymer at dopant levels and the local temperature is measured by monitoring spectral features of the dye. In the ultrasonic technique, ultrasonic velocity in a hot body is converted to temperature by means of a precisely measured velocity-temperature relation. In infrared pyrometry, the radiant energy emitted by the polymer is used to retrieve the temperature inside the material. In this work, we describe an original radiation thermometer for polymer temperature sensing.

Radiation thermometers have been used to measure process stream temperatures for some time in processing industries such as the steel industry, the aluminium industry, and the glass industry. However, in the field of polymer processing, the application of radiation thermometry has drawn only a limited amount of attention from researchers, and its successful application to measure either bulk or detailed process stream temperatures remains a challenging task. Due to the restricted theoretical developments as well as hardware limitations, applying radiation thermometers has at present only been able to provide thermal information about the process stream in terms of an average or bulk temperature, but not about the detailed temperature distribution inside the polymer melt. Beyond the limitation to bulk temperature measurements, another serious drawback of the present thermometers is their limitation to high-temperature targets (e.g. T > 120 °C). This is due to the limited transmission behaviour of the employed optical fibres to the visible and the near-infrared spectral bands. Mid- and far-infrared optical fibres do exist (such as fluoride and chalcogenide glasses) but they are expensive, very fragile, and therefore not appropriate for harsh industrial environments [6].

To carry out remote low-temperature radiometry in the polymer processing industry, we devised a new radiometric unit based on the employment of a dielectric-coated silver hollow waveguide [7, 8]. In radiation thermometry below 120 °C, the dielectric coated metallic waveguide holds transmission efficiency to as high as 50%, which is much higher than any other optical fibre. The waveguide consists of silver and dielectric films deposited on a glass supporting tube. So long as mechanical flexibility is not required for the radiation guide, the dielectric-coated hollow waveguide is the preferred choice for remote thermometry in lower temperature ranges. To date, the hollow waveguide technology has mainly been used in infrared laser delivery systems including laser surgery and material processing [9, 10]. Its use in thermometry has been limited to a few laboratory experiments, using blackbody sources, aiming to investigate the ability of hollow waveguides to monitor low temperatures [11, 12]. The new radiometric unit was designed to measure the bulk temperature inside the polymer, as well as the polymer surface temperature. This new approach is based on the polymer semi-transparency in the spectral band of the photon detector, and on the temperature gradient within the polymer thickness. Thermal information at the polymer surface is a particular advantage of the new radiometric system over commercially available thermometers. This advantage may be useful to obtain a better understanding of the nature of thermal contact between polymer and mould [13, 14], or to get rid of background spurious energy emissions in thin polymer streams (see section 2). Surface temperature measurement may also be employed to retrieve the detailed temperature profile through the polymer thickness using algorithms for ill-posed inverse problems [15-17].

# **2.** Optical considerations for polymer radiation thermometry

Radiation thermometry in the polymer industry involves the evaluation of the spectral emission characteristics of the polymer to be measured. The energy emitted by a polymer material is not evenly distributed in the infrared spectrum. Polymers are spectrum selective materials [1, 2]. By observing the wavelengths at which peak energy is emitted, an instrument sensitive to that wavelength can be selected. This selection is most critical for thin-film polymers for which the thermal radiation detected by the infrared probe is generated not only from the melt polymer film, but also from the surrounding solid surface or background. Selection of the wavelength of peak energy emission is also critical for surface temperature measurement of thicker polymers when the temperature profile through the film thickness is not uniform. For example, polypropylene is partially transparent (about 75% ( $\tau$ )) at most wavelengths between 2 and 16  $\mu$ m except for a few wavelengths at which strong absorption bands exist. Figure 1 shows the overall transmission spectrum of 25 and 250  $\mu$ m thick polypropylene specimens. A fundamental carbon-hydrogen (C-H) absorption band at 3.4  $\mu$ m causes transmission to be zero. From an infrared radiometric point of view, this represents a special region where thin plastic films are opaque. Using an infrared thermometer with a selective narrow band filter in this region, it is possible to accurately measure the film surface temperature rather than the combination of the film and background temperatures. Thus, using the transmission data of figure 1 and assuming a reflectance of 4% ( $\rho$ ), emissivity ( $\varepsilon$ ) can be calculated for polyethylene at 3.4  $\mu$ m:  $\varepsilon$  =  $1 - \rho - \tau$  or, 1 - 0.04 - 0 = 0.96. Since  $\tau$  decreases and  $\varepsilon$  increases as thickness increases, thermometer spectral response becomes less important with thicker polymer films, unless there is a need to measure the surface temperature. In general, thicknesses of less than 2.5 mm require consideration of spectral emission, which should be analysed with a spectrometer to determine the best wavelengths for noncontact temperature measurement. Similarly, in the case of polyester and other ester related polymers, there is a strong C–O absorption band at 7.9  $\mu$ m, whereas fluoro-polymers show strong C-F absorption in this region. In measuring these films, it is necessary to use a radiometric sensor with a selective narrow-band filter at 7.9  $\mu$ m. Some polymers can be measured only at 3.4  $\mu$ m, some can be measured only at 7.9  $\mu$ m, while others can be measured at either The three polymer groups are listed below: wavelength.

3.4 μm	3.4 or 7.9 $\mu$ m	7.9 μm
Polyamide Polyethylene Polypropylene Polystyrene Nylon Ionomer Polytbutylene Glassine	PVC Acrylic Polyurethane Polycarbonate	Polyester PTFE Polyimide Cellophane Cellulose acetate Fluoroplastic

In this paper, we only consider the conception of a thermometer able to detect the radiation emitted in the 3.4  $\mu$ m spectral region. The thermometer may operate either with or without a narrow band pass (NBP) filter at 3.4  $\mu$ m to measure either the surface or bulk temperature of a polymer film. For surface temperature measurement, the thermometer



Figure 1. Transmission spectra of 25 (thin solid curve) and 250  $\mu$ m-thick (bold solid curve) specimens of polypropylene. Polypropylene exhibits an absorption peak at 3.4  $\mu$ m, whereas it is transparent at 7.9  $\mu$ m.

can be operated only for the polymers of the first or second group listed above. A radiometric unit sensitive to the 7.9  $\mu$ m wavelength band may be similarly designed for surface temperature measurements of polymers of the second and the third groups above.

## 3. Thermometer design

A thermometry system, using a dielectric-silver-coated glass hollow waveguide, was devised and examined for continuous operation in an injection moulding process. One can assume for this kind of application that the polymer stream temperature is mainly between 30 and 300 °C. The infrared system consists of a detector head, sensing probe containing a hollow waveguide, and signal-processing unit.

Figure 2 is a diagram of the probe installed in the moving side of the injection mould along with the detector head. The hollow waveguide, incorporated inside the ejection pin, gathers the thermal radiation emitted from the hot polymer and transmits this energy to the photon detector. The employed waveguide consists of a silver film deposited on the inside of a smooth glass supporting tube, and a single fluorocarbon-polymer (FCP) film that is transparent at the desired wavelength. It was manufactured and optimized to meet our needs by a research group at Tohoku University. The concept of this type of waveguide is based on the fact that though metal-tubing fibres exhibit high attenuation, an inner dielectric coating that is properly designed reduces the attenuation loss drastically. The optimum thickness of the dielectric film depends on its refractive index and the desired wavelengths to be transmitted (3.4  $\mu$ m spectral region in the current study). A schematic illustration of the cross structure of a waveguide after deposition of the guiding layers is shown in figure 3. The waveguide has an inner diameter of 4 mm, an external diameter of 6 mm, and a length of 40 cm. Its transmission losses are smaller than 2 dB m<sup>-1</sup> in the 2–4  $\mu$ m spectral range, so that the attenuation due to the employed 40 cm-long pipe portion is quite acceptable. A Teflon sleeve is inserted between the waveguide and the inside of the ejection pin to absorb mechanical shocks. The waveguide is coupled directly to the detector cell-housing window. The direct coupling is quite efficient, but may be improved by inserting an optical lens between the detector head and the waveguide face.

The probe is an ejection pin made with the same P20 steel grade as the mould material. It is machined through its axis to contain the hollow waveguide. It plays the role of shielding the waveguide from mechanical shocks and excessive temperature increase. A circular cavity (diameter 10 mm,



Figure 2. Geometry details of the waveguide thermometer inserted into the moving half-mould side.



**Figure 3.** A schematic illustration of a hollow waveguide cross-section showing the tube and the guiding layers.

depth 2 mm) is machined at one end of the ejection pin to house a flat sapphire window. Sapphire is selected because it is transparent in the 3.4  $\mu$ m wavelength region, strong at high temperatures, and good for high-pressure applications. The window thickness was calculated to withstand the high pressure inside the mould cavity [18], namely ~7000 psi. An Epotek 353ND epoxy adhesive designed for high-temperature and -pressure applications is employed for assembling the optical window to the ejection pin. The probe is inserted into



**Figure 4.** Relation between the thermometer and blackbody temperature. Squares show the calibration when the optical filter is not inserted into the probe. Triangles show the calibration when an optical filter is inserted into the probe. Circles show for reference the calibration with a highly reflective stainless steel tube.

the injection mould so that the tip of the sensor is flush with the inside cavity surface. The other end of the probe is designed to be connected to the detector head, which in turn is connected to the signal processing unit.

The thermal energy transmitted through the optical waveguide is imaged onto a Judson Technologies indium arsenide (InAs) photovoltaic detector. The latter is sensitive in the 1.0–3.6  $\mu$ m spectral region, with a peak sensitivity at 3.4  $\mu$ m. This spectral response is very convenient for monitoring polymers of the first and second groups, which exhibit high-energy emission at 3.4  $\mu$ m. The photodiode is mounted with thermistors on two-stage thermoelectric coolers and hermetically sealed in a dry nitrogen environment. In order to get a high detectivity, good stability over the required temperature excursion range, and a cutoff wavelength at 3.5  $\mu$ m, the detector is cooled down to a temperature of -30 °C. A preamplifier that converts the current output of the detector into a voltage output is used with a 200 kHz bandwidth and a  $10^4$  V A<sup>-1</sup> gain. The temperature is inferred from the detector output through a calibration curve as discussed below.

A NBP filter transparent to the 3.4  $\mu$ m wavelength through a 140 nm half-bandwidth is inserted between the hollow waveguide and the detector to isolate the radiation emitted by the hot polymer surface. The optical filter is employed only when surface temperature measurement is required. Removing the filter allows measuring the average temperature through a certain optical penetration depth in the polymer. However, in this operating configuration, the spurious radiation emitted by the opposite mould side may affect the measurement of thinpolymer streams.

Prior to carrying out on-line trials, the radiometric device was calibrated using a Mikron M315 blackbody source in the temperature range 30–300 °C. Calibrations were performed with and without insertion of the NBP filter at room temperature (see figure 4). To investigate the effect of the waveguide temperature on the calibration curve, the experiment was again performed after holding the waveguide

in an oven at variable temperatures (<80 °C). The waveguide transmission was not affected by its elevated temperature. We also analysed for reference purposes the usefulness of the FCP-silver-coated glass pipe over the use of a highly reflective metal tube. We performed a comparison calibration using a stainless steel tube without NBP filter insertion. It is obvious from figure 4 that the dielectric-metal-coated waveguide enhances drastically the sensitivity of the remote infrared system in low temperature radiometry.

### 4. Experiments and results

The experiments were carried out on a 250 tonne Husky injection moulding press. Images in figure 5 show the detailed shape of the manufactured polypropylene part. Polypropylene was selected because it exhibits a peak absorbance at the 3.4  $\mu$ m wavelength. This characteristic is useful to test the ability of the new radiometric device in measuring the temperature at the polymer surface. Another reason that motivated the choice of polypropylene is related to its high sensitivity to temperature and inside cavity pressure ranges. Shrinkage and warpage phenomena are in general quite significant for polypropylene during injection moulding [13, 14]. The nominal thickness of the experimental injected part is 2.29 mm, which is quite small compared to the lateral extension of the part. Such dimensions usually favour one-dimensional heat diffusion through the stream thickness in locations far from part non-homogeneities.

The waveguide radiometric unit described above was set into an experimental injection mould (see figure 2) to analyse temperature changes of the polymer flow during the process. The sensing probe was installed in such a way that the sapphire window was flush with the face of the mould cavity. In order to investigate the effect of process conditions on the temperature reading, two other sensors were incorporated beside the infrared probe. Figure 5 shows the relative locations



(b)



**Figure 5.** Shape of the injected polypropylene part and corresponding locations of the thermal sensor (circle on the left side), the waveguide probe (circle in the centre), and the cavity pressure transducer (circle on the right side).

of the three sensors with coloured circles painted on the injected part. The large circle in the centre shows the area where the infrared probe collected the thermal radiation. On the right-hand side, a DME SS-405C standard slide pressure transducer was inserted to record the inside cavity pressure. On the left-hand side, a thermal sensor, which was designed specially in our laboratory for this study, was inserted to monitor the mould temperature  $\sim 1$  mm beneath the cavity surface. Data monitoring for all the sensors was performed at a 500 Hz frequency.

During the experiments, the operating parameters such as injection temperature, hydraulic pressure, mould-cooling-oil temperature and extrusion screw movement were also carefully monitored. Meanwhile the press was kept running in order to maintain it in a stable condition. The hydraulic pressure was set to its lowest level to favour polymer shrinkage and unsticking phenomena at the polymer mould interface. Numerous series of experiments were undertaken for different combinations of the process parameters. In each series, the waveguide radiometric unit was employed with or without the optical filter in order to obtain either the surface or the bulk temperature of the polymer stream. For the sake of clarity, only the results for one trial series are reported in this paper. The series concerned corresponds to a mould cooling oil temperature of 25 °C, and an injection melt temperature of 275 °C.

Since the polymer part thickness was quite small, namely 2.29 mm, the bulk temperature reading might be affected by the background radiation emitted by the opposite side of the mould cavity. This issue was investigated with the overall transmission spectrum of a 2.29 mm thick polypropylene film as recorded by a standard FTIR spectrometer. Spectral scans (see figure 6) revealed that the 2.29 mm thick film is still partially transparent in the sensitive range of the InAs detector. The magnitude of the error introduced by the spurious radiation on the bulk temperature measurement would obviously depend on the polymer and mould temperature levels.

For reliability investigation, the temperature recorded with the waveguide device just before the part was ejected out of the mould, was compared to the temperature recorded with an AGEMA 900 LW infrared camera when the part was outside the mould. A few seconds passed between the time the part was ejected and thermal imaging performed. This delay was related to the time necessary to bring the ejected part in front of the thermography unit. This had a HgCdTe detector sensitive in the 4–14  $\mu$ m spectral band. To avoid having the imaging system capture the background radiation, a NBP filter centred at 9.0  $\mu$ m was incorporated into the optical field of view of the camera detector. The use of the latter filter is justified by the transmission spectrum of the 2.29 mm thick polypropylene film reported in figure 6. The 2.29 mm thick part is completely opaque in the 9.0  $\mu$ m wavelength region. The temperature at the location of the waveguide probe was extracted from the thermal image and then reported in figure 7 together with the surface and bulk temperature histories of the part obtained with the waveguide thermometer. The waveguide thermometer data were also compared, on the same graph, to the temperature history of the mould near the cavity surface by the thermal sensor. Hydraulic pressure, inside cavity pressure, and extrusion screw location recorded during the same injection cycle are reported in figure 8.

The following observations deserve to be pointed out:

• During the filling and the cooling under pressure a good contact is ensured between the polypropylene and the mould, so the heat transfer occurs across a small thermal contact resistance. As soon as the relative pressure becomes equal to zero, the effect of the shrinkage results in the appearance of an air gap between the mould and the polymer. This air gap disturbs the heat transfer near the interface [13, 14]. A consequence of this bad heat transfer at the interface is a sudden drop in the heat flux density crossing the interface between the polymer and the mould. Indeed, the heat from the core of the part, which is cooling, is carried by conduction toward the polymer surface, and in case of good contact, crosses the interface to be evacuated in the mould. On the other hand, if an air gap suddenly occurs between the polymer and the mould, the polymer can be reheated at its surface and an abrupt hump



Figure 6. Transmission spectrum of a 2.29 mm thick polypropylene film. The film is still semi-transparent in the sensitive spectral range of the InAs detector, and opaque in the infrared camera 9  $\mu$ m region.



**Figure 7.** Temperature measurements of the polymer stream inside the cavity for a melt temperature of  $275 \,^{\circ}$ C and a cooling oil temperature of  $25 \,^{\circ}$ C. Curve (1): polymer bulk temperature; curve (2): polymer surface temperature; curve (3): location of the extrusion screw; curve (4): mould temperature near the cavity surface; gray triangle: thermography measurement.



Figure 8. Inside cavity pressure (curve (1)), hydraulic pressure (curve (2)), and extrusion screw location (curve (3)) during the injection cycle.

can be seen on the temperature versus time curve. It can be clearly observed from figure 7 that the surface polymer temperature history is more sensitive to the presence of an air gap than the bulk polymer temperature. In addition, the air gap causes the plastic part to cool more slowly, which is exactly observed in the bulk and surface temperature curves. • The bulk temperature before the appearance of the air gap is greater than the surface temperature. This is due to the transparency of the polymer and a non-uniform temperature profile through the stream thickness. The temperature in the core is higher than at the surface. The infrared probe's reading is dominated by the hot material at the core of the cavity and the opposing wall makes a relatively insignificant contribution toward this measurement. When the polymer becomes unstuck from the cavity surface, the relative behaviour of the bulk and surface temperature is reversed. The surface temperature becomes slightly higher than the bulk temperature. This might be caused by the fact that at that temperature magnitude the error introduced into the bulk temperature by the radiation emitted from the opposite mould cavity side is significant. After the sudden temperature increase, the deviation between the surface and bulk temperatures reduces to become insignificant at the end of the cycle. This is due to the fact that the temperature gradients through the polymer thickness are quasi-null, making the average temperature over the optical penetration depth equal to the surface temperature.

- The polymer stream reaches the infrared probe  $\sim 0.43$  s after the injection cycle begins. It is the time of the maximum temperature (bulk or surface) rise. Time zero is known through the extrusion screw movement reported by curve (3) in figures 7 and 8. Between times 0 and 0.43 s the cavity in front of the infrared probe is empty; the temperature increase is only apparent. It is caused by the multiple reflections over the mould cavity walls of the radiation emitted from the hot polymer when it spurts out of the injection gates.
- The inside cavity pressure has a direct effect on the temperature of the polymer stream. The abrupt pressure fluctuation that occurs just before the pressure reaches a maximum affects instantaneously the temperature versus time curve. A temperature fluctuation occurs at the same moment the pressure fluctuation happens.
- The part temperature measured with thermography, a few seconds after the part was ejected from the mould, is reported by the triangle in figure 8. It is slightly lower than the polymer temperature measured with the waveguide thermometer just before the part is ejected. The reason for this discrepancy must be the delay between the ejection and thermography measurement. However, this measurement remains significant and useful since it gives an idea on the reliability of the new radiometric unit.
- Another indication of the good reliability of the new radiometric unit is the temperature of the mould surface recorded with the thermal sensor. Indeed, near the end of the injection cycle, the polymer temperature (surface or bulk) measured with the waveguide thermometer tends to catch up to the near surface mould temperature. The discrepancy that still remains at the end of the cycle is likely caused by a non-perfect contact between polymer and mould.

## 5. Conclusion

A new remote thermometer has been designed for lowtemperature monitoring in the injection moulding process. The radiometric procedure may also be employed in other applications such as extrusion and blow moulding. The key feature of the new system is the use of a special hollow optical fibre for transmitting the radiation emitted by the target to the photon detector. The advantage of the latter fibre is its high transmission in the mid- and far-infrared bands, which allows its use for low-temperature applications, whereas conventional full-core optical fibres exhibit high transmission loss in those spectral regions. Infrared optical fibres do exist but are very expensive, fragile and not suitable for low-temperature radiometry. The new radiometric device allows the measurement of the bulk temperature inside polymer streams. It is also specifically designed for surface temperature measurement of polymers that are opaque in the 3.4  $\mu$ m wavelength region. A similar system based on the same technology may be easily developed for surface temperature monitoring of polymers opaque in the 7.9  $\mu$ m wavelength region. Surface temperature is an extra piece of information that is provided for the first time in remote radiometry of injection moulding. Its knowledge may give a better insight into the nature of heat transfer at the polymer mould interface. Moreover, it may be used to determine the detailed temperature profile through the stream thickness by using inverse problem algorithms. Extensive use of the new waveguide system in injection moulding has proven that it is an accurate and reliable instrument. Shrinkage and warpage phenomena effects that are usually encountered in such processes were clearly observed in the surface and bulk temperature histories.

### References

- [1] Migler K B and Bur A J 1997 Plast. Eng. October, 27
- [2] Lai G Y and Rietveld J X 1996 Polym. Eng. Sci. 36 1755
- [3] Migler K B and Bur A J 1998 Polym. Eng. Sci. 38 213
- [4] Konno M, Cui A, Nishiwaki N and Hori S 1993 Proc. 51st Annual Technical Conf. (New Orleans, LA: Society of Plastics Engineers) p 2798
- [5] Maier C 1996 Polym. Eng. Sci. 36 1502
- [6] Saito M and Kikuchi K 1997 Opt. Rev. 4 527
- [7] Harrington J A 2000 Fiber Integr. Opt. 19 211
- [8] Matsuura Y and Harrington J A 1995 Opt. Lett. 20 2078
- [9] Cossman P H, Romano V, Sporri S, Altermatt H J, Croitoru N, Frenz M and Weber H P 1995 Lasers Surgery Medicine 16 66
- [10] Gannot I, Schrunder S, Dror J, Inberg A, Ertl T, Tschepe J, Muller G J and Croitoru N 1995 *IEEE Trans. Biomed. Eng.* 42 967
- [11] Alaluf M, Dror J, Katzir A and Croitoru N 1993 J. Phys. D: Appl. Phys. 26 1036
- [12] Saito M, Sato S and Miyagi M 1992 Opt. Eng. 31 1793
- [13] Quilliet S, Le Bot P, Delaunay D and Jarny Y 1997 Proc. Natl Heat Transfer Conf. vol 2 (New York: ASME) p 9
- [14] Delaunay D and Le Bot P 2000 Polym. Eng. Sci. 40 1682
- [15] Rietveld J X and Lai G Y 1994 Proc. ANTEC Conf. (New Orleans: Society of Plastics Engineers) p 836
- [16] Bendada A and Nguyen K T 1999 Proc. 3rd Int. Conf. on Inverse Problems in Engineering (New York: ASME) p 355
- [17] Nguyen K T and Bendada A 2000 Modelling Simul. Mater. Sci. Eng. 8 857
- [18] Chervin J C, Syfosse G and Besson J M 1994 Rev. Sci. Instrum. 65 2719